

# Bruce and Electric Dipole Spin Resonances

## Old Days' Story and

PRL **99**, 246601 (2007)

PHYSICAL REVIEW LETTERS

week ending  
14 DECEMBER 2007

### Hyperfine-Mediated Gate-Driven Electron Spin Resonance

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Magnetic Excitations in Semiconductors - Bridges to the Next Decade

McCombe Fest-Symposium, Buffalo, March 6 – 8, 2008

# Beginning of the Story: 40 years ago

Ninth International Conference on Physics of Semiconductors  
Moscow, Summer 1968

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1 MAY 1967

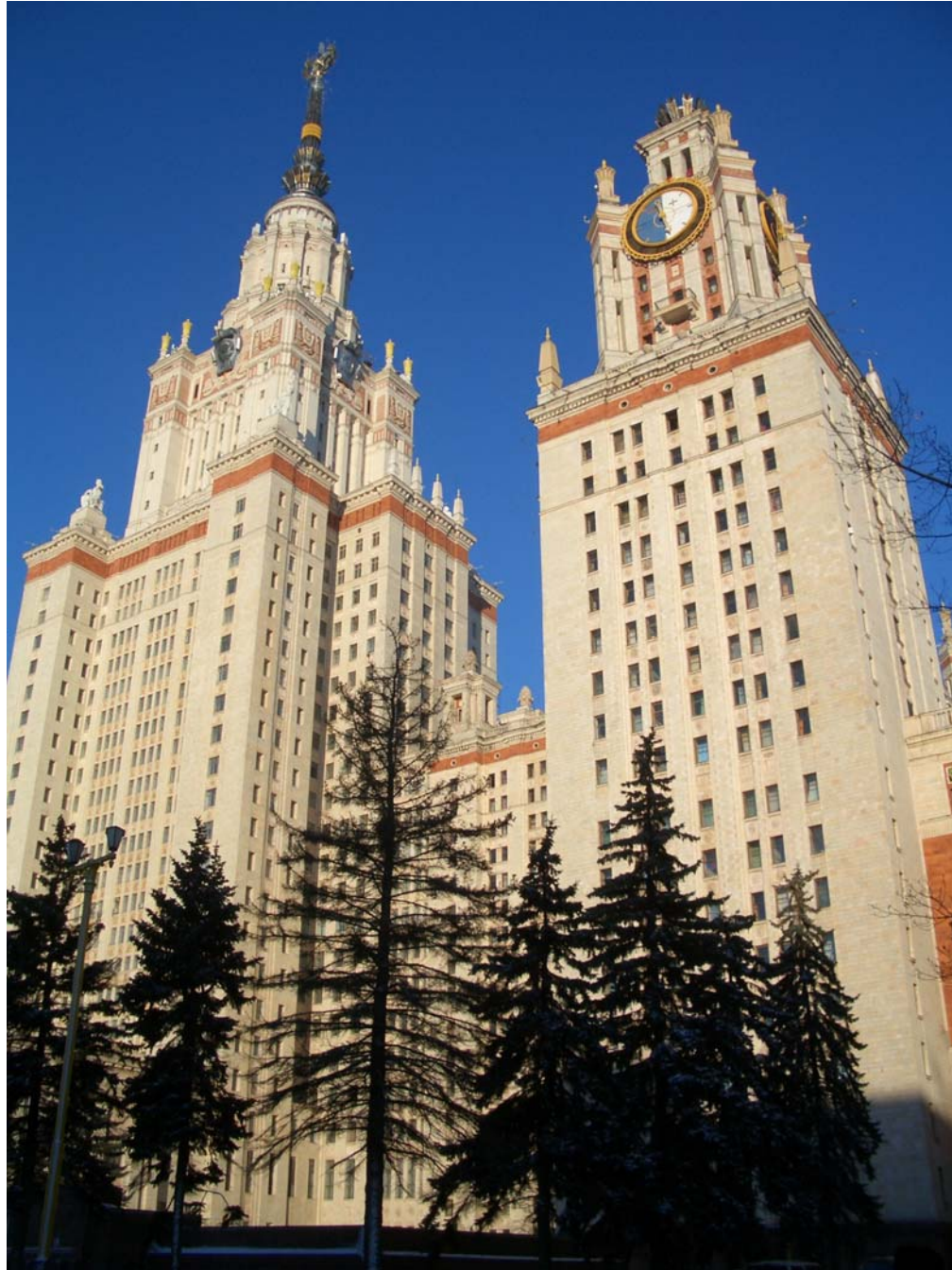
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COMBINED RESONANCE AND ELECTRON  $g$  VALUES IN InSb\*

B. D. McCombe,<sup>†</sup> S. G. Bishop,<sup>†</sup> and R. Kaplan

Naval Research Laboratory, Washington, D. C.

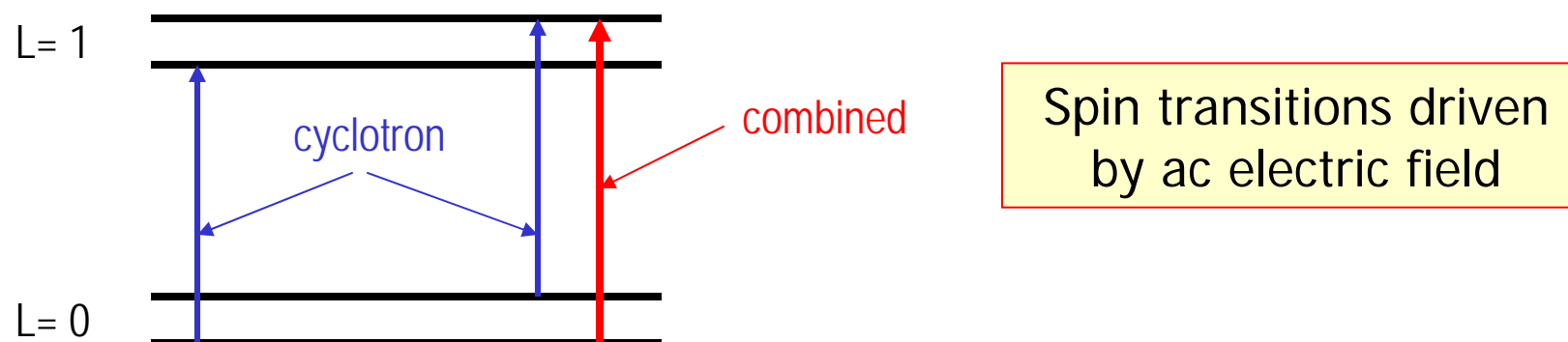
(Received 24 March 1967)





In that paper, McCombe, Bishop, & Kaplan (PRL 1967) reported for InSb:

1. **Discovery** of Electric Dipole transitions at the frequencies  $h\nu_c$  and  $h\nu_c+h\nu_s$   
First the **Cyclotron** Resonance, second the **Combined** Resonance



2. Using them as an instrument for measuring g-factor at L=0 and L=1 Landau levels
3. Establishing a specific **mechanism of the Combined Resonance** (will come to this point)

Afterwards Bruce made the Combined Resonance a powerful tool for measuring g-factors and electron-phonon coupling constants, discovered it in  $\text{Hg}_{1-x}\text{Cd}_x\text{Te}$  (McCombe & Kaplan, PRL 1968), etc.

**Bruce proved the reality of the Combined Resonance convincingly**

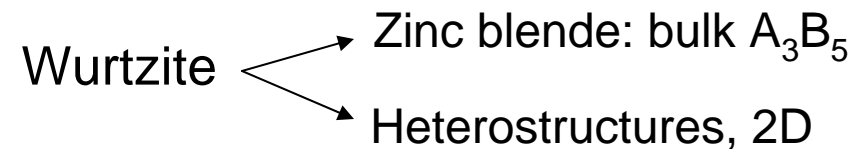
In modern terms:

**Electric Dipole Spin Resonances (EDSR)**

# Why proving was important: Principle and Parameter Values

ER, Sov. Phys. Solid State **2**, 1109 (1960)

**The prediction that EDSR can be orders of magnitude stronger than the magnetically driven spin resonance was accepted skeptically, in particular by the ESR community**



Change from 3D to lower dimensions and confined systems was inspired by two papers:

Stormer, Schlesinger, Chang, Tsui, Gossard, Weimann, PRL **51**, 126 (1983)  
Cyclotron resonance, 2D holes

Stein, von Klitzing, Weimann, PRL **51**, 130 (1983)  
Spin resonance, 2D electrons

Bychkov & ER, Sov. Phys. - JETP Lett. **{\bf 39}**, 78-81 (1984)

Zero-order approach to the description of both systems

## Multiplicity of EDSR mechanisms: Great challenge

$A_3B_5$ , bulk 3D, **intrinsic** mechanisms:

$$H_{SO} \propto \boldsymbol{\sigma} \cdot \boldsymbol{\kappa}, \kappa_z = k_x k_z k_x - k_y k_z k_y, \mathbf{k} \rightarrow \mathbf{k} - e\mathbf{A}/\hbar c \quad \text{Dresselhaus 1955}$$

Dobrowolska, Chen, Furdyna, Rodriguez, PRL **51**, 134 (1983)

$$H_{SO} \propto \mathbf{E} \cdot \mathbf{r}_{SO}, \mathbf{r}_{SO} \propto \boldsymbol{\sigma} \times \mathbf{k}$$

Yafet 1963

Discovered by McCombe et al. 1967

**Extrinsic** mechanisms: puzzling results on n-InSb, Bell, PRL **9**, 52 (1962)

compensated n-Ge, Gershenson et al. JETP Lett. **12**, 139 (1970)

**Inhomogeneous Zeeman** mechanism of spin-orbit coupling,  $H_Z = g(\boldsymbol{\sigma} \cdot \mathbf{B}(\mathbf{r}))$

Pekar & ER, 1965

Reviewed by ER & Sheka, 1991

# Nanoscopic EDSR in a Double Quantum Dot

## Single electron operation

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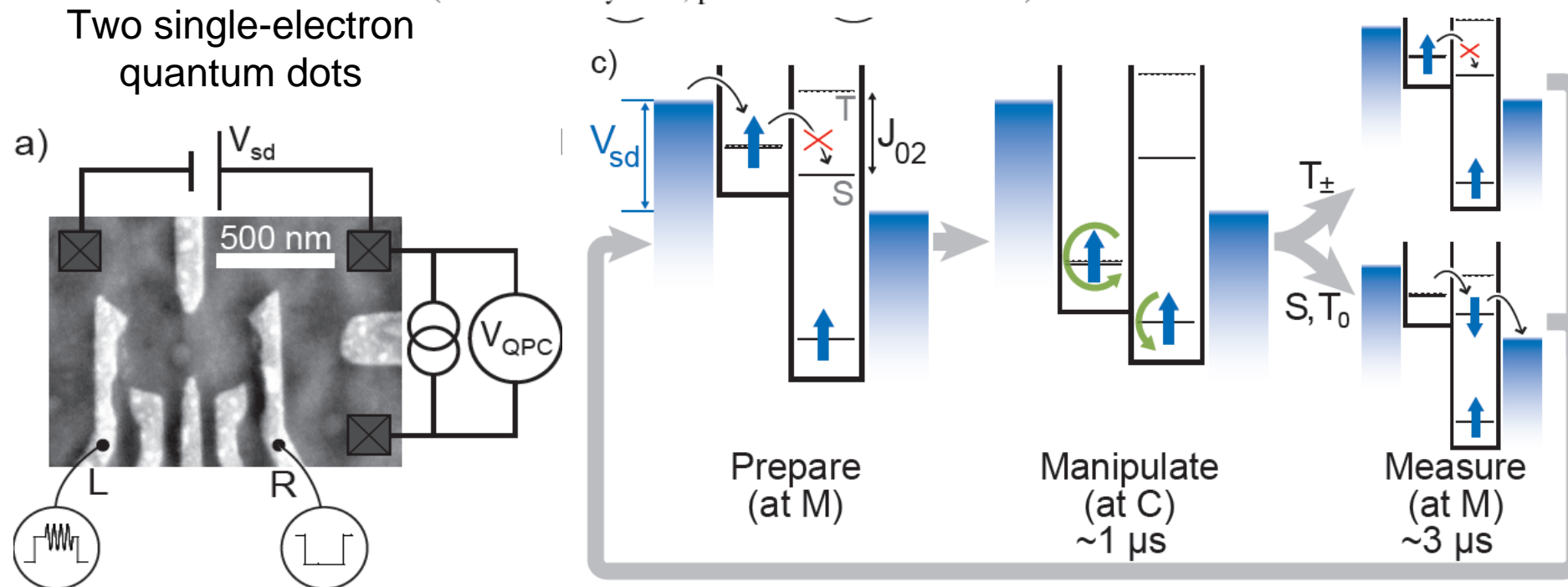
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# Two competing mechanisms of EDSR in a quantum dot

## 1. Time dependent hyperfine interaction – a new mechanism of EDSR

$H_{\text{hf}}(t)$ , in the vibrating quantum dot frame

$$H_{\text{hf}}(t) = A \sum_j \delta(\mathbf{r} + \mathbf{R}(t) - \mathbf{r}_j)(\mathbf{I}_j \cdot \mathbf{S}), \quad \mathbf{R}(t) = -e\mathbf{E}(t) / m\omega_0^2$$

$$\text{Rabi frequency } \Omega_R = \frac{eEA}{\hbar^2 \omega_0} \sqrt{\frac{I(I+1)n_0}{8\pi d}}$$

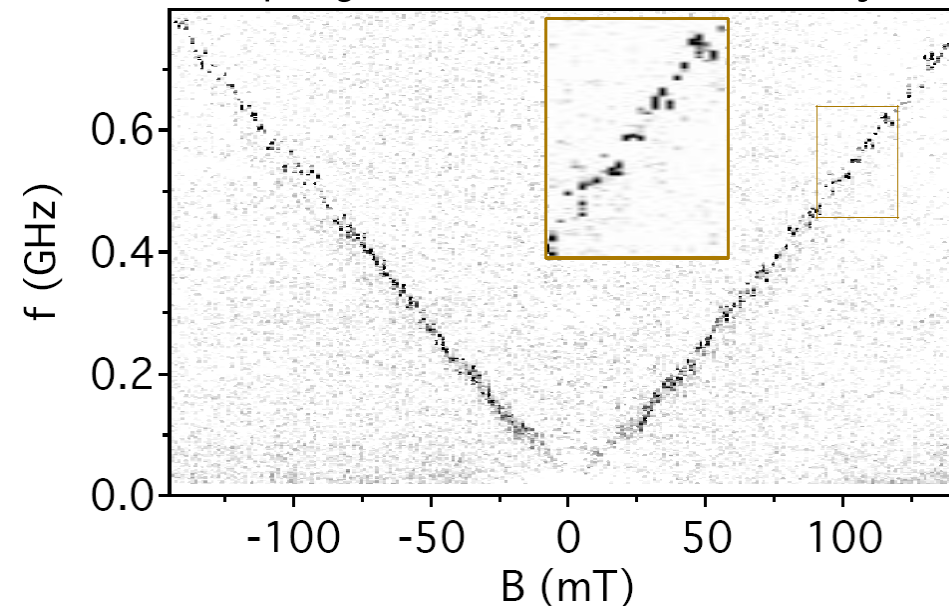
EDSR intensity and  $\Omega_R$  do not depend on  $B$  because  $t$  - inversion is violated

Slope:  $g$ -factor. Darkness: Intensity

## 2. Spin-orbit coupling

$$H_{\text{SO}} \propto (\boldsymbol{\sigma} \cdot \hat{\mathbf{k}})$$

EDSR intensity is proportional to  $B^2$   
because of the Kramers theorem



# Experimental data vs semiclassical theory

Dependence of the current on the pulse duration  $\tau_{\text{EDSR}}$

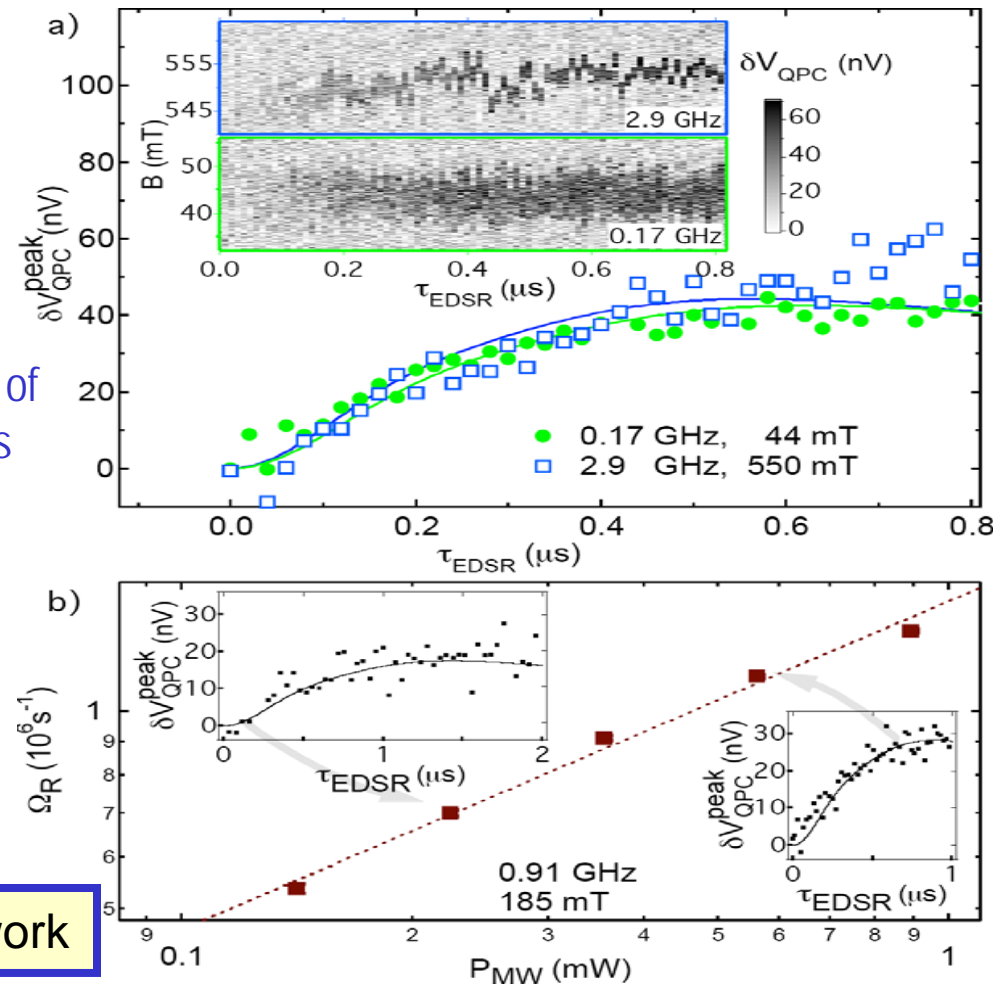
From the curve shape,  $\Omega_R$  can be found

*Notice:* There are no Rabi oscillations because of the averaging over nuclear spin configurations

Rabi frequency dependence on the microwave power  $P_{\text{MW}}$

$$\Omega_R \propto \sqrt{P_{\text{MW}}}$$

Hyperfine mechanism of EDSR is on work



At larger fields  $B$ , spin-orbit mechanism dominates, Nowack *et al.*, Science **318**, 1430 (2007)

# Conclusions

- (i) Old Days' reminiscences,
- (ii) Seminal paper by Bruce et al. (1967),
- (iii) Multiplicity of EDSR mechanisms,
- (iv) Related challenges,
- (v) Nanoscopic single-electron EDSR in quantum dots